Second-Order Nonhomogeneous Equations

Math 230

Solve each linear differential equation by completing the following steps:

- (a) Write the associated homogeneous equation and find its general solution $k_1y_1(t) + k_2y_2(t)$.
- (b) Find any particular solution $y_p(t)$ to the nonhomogeneous equation.
- (c) The general solution to the nonhomogeneous equation is $k_1y_1(t) + k_2y_2(t) + y_p(t)$.

What is the long-term behavior (as $t \to \infty$) of each solution that you find?

1.
$$y'' + 4y = \cos(t)$$

2.
$$y'' + 2y' + y = e^{-t}$$

3.
$$y'' + 6y' + 8y = 2t + e^t$$

4.
$$y'' + 5y' + 6y = \sin(t)$$