First-Order Linear Differential Equations

Math 230

Solve the linear differential equations by completing the following steps:

- (a) Write the associated homogeneous equation and find its general solution $ky_h(t)$.
- (b) Find any particular solution $y_p(t)$ to the nonhomogeneous equation.
- (c) The general solution to the nonhomogeneous equation is $ky_h(t) + y_p(t)$.
- (d) Check your solution by plugging it back in to the nonhomogeneous equation.

$$1. \ \frac{dy}{dt} = 3y + e^{-t}$$

$$2. \ \frac{dy}{dt} = -y + \sin(t)$$

$$3. \ \frac{dy}{dt} = y + e^t$$

$$4. \ \frac{dy}{dt} = y + t + e^{2t}$$